Biosorption Kinetic Models on the Removal of Congo red onto Unripe Calamansi (*Citrus microcarpa*) peels

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ABSTRACT

Unripe calamansi peels were prepared and used as a bioadsorbent in the removal of congo red from an aqueous solution using batch adsorption studies. The efficiency of adsorption was evaluated by varying adsorbent dose and contact time. The removal of congo red increased at higher adsorbent dose and longer contact time. The overall rate of adsorption processes appeared to be in accordance with the pseudo-second order reaction mechanism. Higher initial adsorption rate, extent of surface coverage, and activation energy were favored at a lower adsorbent dose, while the intraparticle diffusion was relatively faster at a higher adsorbent dose. The intraparticle diffusion, Elovich, and MacArthur-Wilson models were adequate in describing the chaotic behavior of the kinetic processes involved in the removal of congo red dye onto unripe calamansi peels.

Keywords: Biosorption kinetics, Pseudo-second order, Elovich, MacArthur-Wilson, Intraparticle diffusion, *Citrus microcarpa*.

INTRODUCTION

Dyes are colored organic compounds which are used in industries that produce textiles, paper, and distilleries. As a result of incomplete binding with fibers during the dyeing process, dyes are found in highly colored wastewaters which pollute bodies of water¹. Due to their high water solubility and ability to color vividly at low concentrations, dyes easily contaminate the wastewater produced by industries². This affects gas solubility and transparency of bodies of water, which have a detrimental effect on aquatic life¹. One of these dyes is congo red which is a common, toxic, and carcinogenic dye used...
for coloration of paper products. Paper industries dispose of congo red in large amounts and are usually found in sediments in polluted canals. When dyes such as congo red enter the water systems, they can cause pollution, consequently harming humans and aquatic organisms.

As such, one way to address this problem is through biosorption. It is a physico-chemical process which makes use of biological materials to adsorb pollutants from aqueous solutions. Currently, activated carbon is one effective yet expensive biosorbent used in treating groundwater and industrial wastes. Agricultural wastes are being considered as an alternative adsorbent compared to other materials due to its availability in large quantities, renewability, and inexpensiveness. Compared to conventional physical and chemical methods, biosorption studies are looking for easier and less costly treatment, often making use of these agricultural wastes as bioadsorbents.

Currently, no biosorption studies have been conducted for calamansi (Citrus microcarpa) peels, although there have been for orange peels, which belong to the same family. Finding potential uses for these discarded peelings may reduce waste and pollution. Hence, this study explores on the removal of congo red from an aqueous solution by unripe calamansi peels in a single component adsorption system at varying adsorbent doses and contact times using spectrophotometry.

In addition, this study attempts to elucidate the mechanisms governing the removal of congo red, and to find a suitable mathematical model for the kinetics of the removal involving adsorbent dose and contact time. In particular, comparison on the removal of congo red from an aqueous solution using calamansi peels under constant pH, dye concentration, and temperature will be made. Only unripe calamansi peels as adsorbent with congo red as the adsorbate were used in this study. Furthermore, factors such as the dye concentration, pH, and temperature were kept constant at 0.1 g/L, 4.00, and room temperature (27°C), respectively. The biosorptive properties of calamansi peels were measured across different contact times, namely 10, 20, 30, 40, 50, and 60 min under 0.25 g and 0.50 g adsorbent doses. The mechanisms of adsorption and potential limiting steps will be described using several equations, namely the pseudo-first order, pseudo-second order, Elovich, MacArthur-Wilson, and intraparticle diffusion nonlinear kinetic models.

Nonlinear models, in general, are more difficult to specify, identify, and estimate than linear models, and it involves nonlinear iterative processes in determining the solution. Gauss-Newton, as one of the iterative methods employed in classic nonlinear regression analysis, was considered in estimating the parameters of nonlinear models in this study. The adequacy and sufficiency of the various models were individually assessed. It is important to be able to predict the rate at which hazardous wastes are removed from an aqueous solution in order to design appropriate adsorption treatment systems. Moreover, exhaustive exploration on the adsorption kinetics involving wastewater treatment is important in providing better understanding of the reaction pathways and possible mechanisms involved.

The use of commercial water treatment processes such as activated carbon is limited in the textile industry due to the high cost of production and problems with regeneration. Hence, this necessitates a need for cheaper and more efficient alternative methods, and one of these is biosorption. One reason that makes biosorption a potential alternative to the current commercial methods is the abundance of biomass. Utility of calamansi peels as bioadsorbent would help in the reduction of agricultural waste and pollution. In a system design perspective, aggregate analysis of varying adsorption rates is a prerequisite for practical application and this requires examination of the controlling mechanism of the adsorption process which includes the mass transfer, chemical reaction, and diffusion control. As such, several adsorption kinetic models were tested using the obtained experimental data. Therefore, the study could provide potential alternatives to other dye-removal methods like membrane filtration, reverse osmosis, coagulation or flocculation, and fenton reagents which are not economically feasible. Considering the lack of studies exploring calamansi peels as bioadsorbent, the study will provide baseline information on the adsorptive properties of calamansi peels.
MATERIALS AND METHODS

Preparation of Adsorbents and Adsorbate

Calamansi Peels

Citrus microcarpa is a fruit available in the Philippines year-round, but is most abundant from August to October\(^{10}\). Due to its varied uses, the plant is cultivated both on a large and small scale throughout the country. Unlike oranges, which are also part of the Rutaceae family, calamansi fruit peelings have not been tested for adsorptive properties.

Five kilograms of unripe calamansi was procured from Villa Colongan, Barangay Colongan, Ibaan, Batangas, Philippines and subsequently peeled after two days. The peels were washed with distilled water to remove impurities and other particles, cut into small pieces, and dried in an oven at 100°C for 90 min\(^{8}\). The dried peels were then crushed using a mortar and pestle, then grounded into granules and sifted through a 1.00 mm mesh in order to control particle size. Degraded cells offer a larger available surface area and intracellular component resulting to increase in the availability of more surface binding sites and modifies the functional groups present in the cell wall\(^{11}\). Subsequently, the sifted granules were washed with distilled water and decanted until the supernatant fluid had a comparable absorbance to that of distilled water. The adsorbent was dried again in an oven for 80 min at 50°C and subsequently stored in a desiccator until it was used in the experiment\(^{12}\).

Congo red and Point of Zero Charge

Congo red (C\(_\text{32}H\text{22}N\text{6Na}_\text{2O}_\text{6S}_\text{2}\); 696.68 g/mol) is an anionic direct diazo dye that is mainly used for paper coloration in the paper industry\(^3\), and about 15% of congo red ends up in wastewater\(^{13}\). It is the sodium salt of benzidine-diazo-bis-1-naphthylamine-4-sulfonic acid and is known to degrade into benzidine, which is a carcinogen\(^{14}\). The treatment of congo red contaminated wastewater can be implicated due to its complex aromatic structure\(^{15}\), providing the dye physico-chemical, thermal and optical stability, and resistance to biodegradation and photodegradation\(^{16,17}\).

The point of zero charge (pH\(_\text{pz}\)) is the pH at which the surface of an adsorbent has a net charge of zero, and the surface of an adsorbent will be positive and will attract anions if the pH is lower than pH\(_\text{pz}\), while a negatively charged surface will favor the adsorption of cationic substances if the pH is above the pH\(_\text{pz}\). At pH below the isoelectric point, a dye exists predominantly in its molecular form, while above the isoelectric point, it exists with a higher proportion in its dissociated form. The isoelectric point of congo red is 3, thus it would be negatively charged at pH range of 5.0-10.0\(^{18,19}\). Considering the anionic nature of congo red, it can be said that setting the stock solution to an acidic pH will theoretically allow better adsorption. Rice husk ash was observed to exhibit a high adsorption capacity on congo red at pH 4.0\(^{20}\).

Congo red solution with a concentration of 0.1 g/L was prepared by dissolving 0.1 g congo red in 1 L acetate buffer with a pH of 4.00. A buffer solution with a pH of 4.00 was prepared using 0.1 M NaOH and 1 M acetic acid\(^{12}\). The flask was wrapped in aluminum foil and stored inside an icebox until it was needed.

Establishment of Calibration Curve

A calibration standard for the congo red was prepared by mixing the dye with acetate buffers resulting into five different concentrations which range from 5 to 85 ppm of three replicates per trial. The absorbance for each calibration solution was then determined using a UNICO UV-Vis spectrophotometer set at \(\lambda_{\text{max}} = 500\) nm with a uniform pathlength of 1 cm for all the trials\(^{21}\). Simple linear regression analysis was employed to generate the calibration curve.

Batch Adsorption Study

From the stock solution of 0.1 g/L congo red, 70 mL was transferred to a 250-mL beaker, and then 0.50 g of adsorbent was added to the solution which was mixed using a magnetic stirrer operating at 500 rpm. A volume of 8 mL sample was taken from the mixture using a syringe at 10-min intervals for 60 min. The samples were then filtered using Whatman\(^6\) nitrocellulose membrane filters of pore size 0.45 µm to separate the adsorbent from the solution\(^{12}\), the absorbance of each sample was subsequently measured using a UNICO UV-Vis spectrophotometer set at \(\lambda_{\text{max}} = 500\) nm\(^8\). The same procedure was done for the 0.25 g adsorbent.
dose. Two replicates for each adsorbent dose were prepared.

**Percent Removal of Dye**

For each absorbance measurement, the corresponding molar concentration was then calculated using (1). According to Beer’s law, the product of molar absorptivity and pathlength is replaced by the slope obtained in the calibration curve.

\[
\text{Molar concentration} = \frac{\text{Absorbance}}{\text{Molar absorptivity} \times \text{Pathlength}} \quad \text{(1)}
\]

In order to determine the magnitude of the effects of the adsorbent on congo red, the percent removal for each trial with respect to the initial mean molar concentration can be derived from the nontreated pre-filtration using (2).

\[
\% \text{ Removal} = \frac{C_i - C_f}{C_i} \times 100\% \quad \text{(2)}
\]

Using the calibration curve, the final molar concentration was calculated and subsequently the percent removal of the dye was computed. For the given initial and final concentrations of the dye, denoted as \(C_i\) and \(C_f\), respectively, the percent removal can be computed using (2)\(^4\).

**The Bioadsorption Kinetic Models**

The functional relationship between contact time and the amount of congo red adsorbed, with a levelling of the increase of the amount of dye adsorbed at some contact time value, depicts a chaotic nonlinear interacting relationship. A nonlinear model was required to capture this phenomenon.

**The Pseudo-First Order Kinetic Model**

The pseudo-first order kinetic model is given as

\[
\frac{da_t}{dt} = c_1 (a_s - a_t) \quad \text{(3)}
\]

where \(a_t\) (mg g\(^{-1}\)) is the amount of dye adsorbed at time \(t\), \(a_s\) (mg g\(^{-1}\)) is the adsorption capacity at equilibrium, \(c_1\) (min\(^{-1}\)) is the pseudo-first order rate constant, and \(t\) (min) is the contact time. The general solution to this pseudo-first order model is

\[
\log(a_s - a_t) = \log(a_s) - \frac{c_1}{2.303} \times t \quad \text{(4)}
\]

**The Pseudo-Second Order Kinetic Model**

The pseudo-second order kinetic model\(^{22}\) is given as

\[
\frac{t}{a_t} = \frac{1}{c_2(a_s)^2} + \frac{1}{a_s} \times t
\]

**Table 1: Linearized form of the different kinetic models for initial parameter estimation procedure**

<table>
<thead>
<tr>
<th>Model</th>
<th>Linearized form</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pseudo-first order</td>
<td>[\log(a_s - a_t) = \log(a_s) - \frac{c_1}{2.303} \times t]</td>
</tr>
<tr>
<td>Pseudo-second order</td>
<td>[\frac{t}{a_t} = \frac{1}{c_2(a_s)^2} + \frac{1}{a_s} \times t]</td>
</tr>
<tr>
<td>Elovich</td>
<td>[a_t = \frac{1}{\beta} \ln(\alpha \beta) + \frac{1}{\beta} \ln t]</td>
</tr>
<tr>
<td>MacArthur-Wilson</td>
<td>[\ln \left(1 - \frac{a_t}{a_s}\right) = -\beta_t t]</td>
</tr>
<tr>
<td>Intraparticle Diffusion</td>
<td>[a_t = k_{id} \times t^\frac{1}{2} + C]</td>
</tr>
</tbody>
</table>
\[
\frac{da_t}{dt} = c_2 \left( a_e - a_t \right)^2 \tag{5}
\]

where \( a_t \) (mg g\(^{-1}\)) is the amount of dye adsorbed at time \( t \), \( a_e \) (mg g\(^{-1}\)) is the adsorption capacity at equilibrium, \( c_2 \) (g mg\(^{-1}\) min\(^{-1}\)) is the pseudo-second order rate constant, and \( t \) (min) is the contact time. The general solution to this second order differential equation is defined as

\[
\frac{t}{a_t} = \frac{1}{c_2(\alpha e)^2} + \frac{1}{\alpha e} t \tag{6}
\]

The Elovich Model

The Elovich model\(^3\) is defined as

\[
\frac{da_t}{dt} = \alpha e^{-\beta a_t} \tag{7}
\]

The solution to this differential equation describes the activated chemisorptions\(^24\) and is defined by

\[
a_t = \frac{1}{\beta} \ln(\alpha \beta) + \frac{1}{\beta} \ln t \tag{8}
\]

where \( a_t \) (mg g\(^{-1}\)) is the amount of dye adsorbed at time \( t \), \( \alpha \) (mg g\(^{-1}\) min\(^{-1}\)) is defined as the initial adsorption rate, \( \beta \) (g mg\(^{-1}\)) is the extent of surface coverage and activation energy for chemisorption, and \( t \) (min) is the contact time.

The MacArthur-Wilson Model

The MacArthur-Wilson model is a two-parameter negative exponential model\(^25\) which takes the form

\[
a_{t_i} = \beta_o (1 - e^{-\beta_1 t_i}) + \varepsilon_i \tag{9}
\]

where \( a_{t_i} \) (mg g\(^{-1}\)) is the amount of dye adsorbed at time \( t_i \), \( \beta_0 \) (mg g\(^{-1}\)) is a parameter defined as the asymptote or potential maximum, \( \beta_1 \) (min\(^{-1}\)) is defined as the rate at which the response variable approaches its potential maximum, \( t \) (min) is the contact time, and \( \varepsilon_i \) (mg g\(^{-1}\)) is the random error term. The linearized form of (9) is defined as

\[
\ln \left( 1 - \frac{a_{t_i}}{\beta_0} \right) = -\beta_1 t \tag{10}
\]

Intraparticle Diffusion Model

Another functional relationship identified to some adsorption processes is that the uptake varies almost proportionally with \( t^{1/2} \) rather than with the contact time, \( t \). The Weber-Morris plot examines the possible relationship between \( a_t \) and \( t^{1/2} \) using the equation

\[
a_t = k_{id} t^{1/2} + C \tag{11}
\]

where \( a_t \) (mg g\(^{-1}\)) is the amount of dye adsorbed at time \( t \), \( k_{id} \) is the intraparticle diffusion rate constant. The intercept, \( C \), represents the thickness of boundary layer, a larger intercept suggests a greater boundary layer effect because of the instantaneous utilization of the readily available adsorbing sites on the adsorbent surfaces\(^26\).

The Gauss-Newton Method

The proc nlin (nonlinear regression procedure) of SAS (Statistical Analysis System) was...
Fig. 2: Linear plots using (a) pseudo-first order, (b) pseudo-second order, (c) Elovich, (d) MacArthur-Wilson, and (e) intraparticle diffusion kinetic model.

Fig. 3: Comparison of the best-fit kinetic models on the effect of contact time on the adsorption of congo red onto (a) 0.5 g and (b) 0.25 g adsorbent dose of calamansi peels.

Obs- observed experimental values, MAW-MacArthur-Wilson, IPD-intraparticle diffusion.
used to fit the models and estimate the parameters. In software computing algorithms such as SAS, in finding the least squares estimator, in a nonlinear model, one of the most often methods used is the Gauss-Newton procedure. This method is iterative and requires starting value estimates for the parameters\(^5\). Inference on the coefficients using this method is based on the asymptotic variance-covariance matrix of the regression coefficients. Convergence of the parameter estimates depends on the specified initial values. Poor starting points can result the procedure to move in an undesired direction, and so convergence is never met. Hence, transformation of a nonlinear model to a linear form in estimating the parameters by linear regression is a possible solution and was employed in this study, and subsequent values obtained were taken as initial estimates. Table 1 summarizes the linearized form of the different nonlinear kinetic models employed in this study.

Table 2: Parameter estimates of the adsorption kinetic models at varying adsorbent doses

<table>
<thead>
<tr>
<th>Model</th>
<th>Parameter</th>
<th>Adsorbent Dose Levels</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>0.5 g</td>
<td>0.25 g</td>
<td>0.5 g</td>
</tr>
<tr>
<td>Pseudo-first order</td>
<td>(a_e) obs (mg g(^{-1}))</td>
<td>2.800</td>
<td>2.370</td>
<td>(a_e) pred (mg g(^{-1}))</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.5 g</td>
<td>0.25 g</td>
<td>0.5 g</td>
</tr>
<tr>
<td>Pseudo-second order</td>
<td>(a_e) obs (mg g(^{-1}))</td>
<td>2.800</td>
<td>2.370</td>
<td>(a_e) pred (mg g(^{-1}))</td>
</tr>
<tr>
<td>Elovich</td>
<td>(\alpha) (mg g(^{-1}) min(^{-1}))</td>
<td>10.69</td>
<td>2.17x10(^{14})</td>
<td>(\beta) (g mg(^{-1}))</td>
</tr>
<tr>
<td>MacArthur-Wilson</td>
<td>(B_0) (mg g(^{-1}))</td>
<td>2.562</td>
<td>2.347</td>
<td>(B_1) (min(^{-1}))</td>
</tr>
<tr>
<td>Intraparticle Diffusion</td>
<td>(k_{id}) (mg g(^{-1}) min(^{-1/2}))</td>
<td>0.148</td>
<td>0.022</td>
<td>(C) (mg g(^{-1}))</td>
</tr>
</tbody>
</table>

Table 3: Error analysis of the different adsorption kinetic models at varying adsorbent doses

<table>
<thead>
<tr>
<th>Model</th>
<th>SSE 0.5 g</th>
<th>SAE 0.5 g</th>
<th>SAE 0.25 g</th>
<th>ARE 0.5 g</th>
<th>ARE 0.25 g</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pseudo-first order</td>
<td>2.472</td>
<td>4.035</td>
<td>2.214</td>
<td>60.721</td>
<td>12.012</td>
</tr>
<tr>
<td>Pseudo-second order</td>
<td>7.286</td>
<td>8.351</td>
<td>0.782</td>
<td>6.676</td>
<td>0.412</td>
</tr>
<tr>
<td>Elovich</td>
<td>0.168</td>
<td>1.352</td>
<td>0.132</td>
<td>4.594</td>
<td>0.470</td>
</tr>
<tr>
<td>MacArthur-Wilson</td>
<td>0.464</td>
<td>2.277</td>
<td>0.139</td>
<td>7.667</td>
<td>0.472</td>
</tr>
<tr>
<td>Intraparticle Diffusion</td>
<td>0.109</td>
<td>1.008</td>
<td>0.181</td>
<td>0.411</td>
<td>0.078</td>
</tr>
</tbody>
</table>

SSE - Sum of Squares of the Errors; SAE - Sum of the Absolute Errors; ARE - Average Relative Error
Table 4: Differential forms of the second-order derivatives of the kinetic models

<table>
<thead>
<tr>
<th>Model</th>
<th>Second-order derivative</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elovich</td>
<td>(-\frac{1}{\beta t^2})</td>
</tr>
<tr>
<td>MacArthur-Wilson</td>
<td>(-\beta_0 \beta_1 \frac{t \cdot e^{-\beta_1 t}}{t^2})</td>
</tr>
<tr>
<td>Intraparticle diffusion</td>
<td>(-\frac{k_{id}}{4t^{3/2}})</td>
</tr>
</tbody>
</table>

**Error Analysis**

Since the parameter estimation procedure involves nonlinear models, three different error functions of nonlinear regression were utilized to evaluate the adequacy of the best-fit biosorption kinetic model to the experimental data.

**Sum of Squares of the Errors (SSE)**

The most commonly employed error function is SSE, and is defined as

\[
\text{SSE} = \sum_{i=1}^{n} \left( \frac{a_{e,pre} - a_{e,obs}}{a_{e,obs}} \right)^2_i 
\]

where \(a_{e,pre}\) and \(a_{e,obs}\) are the predicted and the observed values (mg g\(^{-1}\)) at equilibrium, respectively, and \(n\) is the number of observations.

**Sum of the Absolute Errors (SAE)**

Parameter estimates employing the SAE describe a better fit as the value of the errors increases as it favors the fit towards the high-concentration observations. The expression for SAE is defined as

\[
\text{SAE} = \sum_{i=1}^{n} \left| a_{e,pre} - a_{e,obs} \right|_i 
\]

**Average Relative Error (ARE)**

The average relative error function attempts to minimize the fractional error distribution across the entire range of observations, and is computed using the expression

\[
\text{ARE} = \frac{100}{n} \sum_{i=1}^{n} \left| \frac{a_{e,pre} - a_{e,obs}}{a_{e,obs}} \right|_i 
\]

... \(\text{(14)}\)

**RESULTS AND DISCUSSION**

The uptake of congo red dye continues to increase until it reaches the equilibrium, for which such phenomenon is typical from the presence of several surface sorption sites, which gradually get saturated with the dye at increasing contact time. The mean removal of congo red revealed a relatively slow initial rate during the first 10- and 20-min intervals \((p>0.05)\), and does not differ between the two adsorbent doses \((p>0.05)\). This is in contrast to the rapid initial adsorption of congo red taking place within the first 20-min interval using chitosan, after which the adsorption slowed down and then almost reached equilibrium at 120 min\(^2\). Beyond the 20-min interval, the removal rate gradually increases, and eventually remains constant for the 0.25 g adsorbent dose as illustrated in Figure 1. However, for the 0.5 g adsorbent dose, removal rate continues to rise until the 50-min interval, and eventually starts to gradually remain constant. The mean amount of dye adsorbed during the 50- and 60-min intervals significantly differ between the two adsorbent doses \((p<0.001)\).

Figure 1 describes the uptake of congo red as it increases up to a certain threshold and then remains almost unchanged. The possible presence of repulsive forces between adsorbate molecules on the solid and bulk phases might contribute to the observed moderate rates of adsorption as it approaches the equilibrium. The equilibrium contact time for 0.5 g and 0.25 g adsorbent doses was observed at 50 min and 30 min, respectively \((p<0.01)\). Adsorption curves are single, smooth, and continuous leading to saturation and indicate the possible monolayer coverage on the surface of adsorbents by the dye molecules. Due to the rapid adsorption of all available sites and a relatively small amount of absorbent used, removal efficiency of congo red decreased; an increase in the amount of adsorbent may therefore reverse adsorption trend. The percentage removal of congo red remarkably increases at an increasing dose. An increase in the dose from 0.25 g to 0.5 g resulted to 33-40% increase in the percent removal. This is possibly explained by...
the increase in the surface area for dye bindings and availability of additional sorption sites\textsuperscript{29, 31, 32}.

**Parameter Estimates and Analysis**

Initial parameter estimates for the varying nonlinear kinetic models employed in this study were obtained using the respective linearized form as presented in Table 1. In the pseudo-first order kinetic model, the linear plots of $\log (c_t - c_e)$ against $t$ is reflected in Figure 2(a). From these plots, the value of $c_1$ in the pseudo-first order kinetic model was determined, and is given in Table 2. Due to the inherent disadvantage of correctly estimating the equilibrium amount adsorbed as obtained from the linearity of the curve, the relationship does not necessarily reflect the pseudo-first order mechanism. Further, the $q_e$ values obtained from the linear plots are different from the observed values, the pseudo-first order adsorption kinetic model is inadequate to describe the given rate processes as justified by the coefficients of determination ($R^2$) significantly deviating from unity.

Figure 2(b) describes the linear plots of $\frac{t}{c_t}$ against $t$ in the pseudo-second order kinetic model. The estimate of the constant, $c_2$, was obtained from these linear plots, and is given in Table 2. It is important to note that the $q_e$ observed and predicted values obtained in the pseudo-second order biosorption kinetic model are almost the same ($R^2=0.99$) which suggests that the adsorption phenomenon can be modelled approximately using the pseudo-second order kinetic equation for the different adsorbent doses. As such, the equilibrium system capacity for the pseudo-second order is relatively more reasonable compared to the pseudo-first order when predicted results were compared with experimental measurements. The pseudo-second order model provides the best correlation in the system processes indicating that the overall rate of congo red adsorption processes appear to be governed by the chemical process in accordance with the pseudo-second order reaction mechanism.

The pseudo-second order equation provides the best correlation for the kinetic process while the Elovich model adequately fits the experimental measurements well at lower adsorbent dose as depicted in Figure 2(c). Results of Elovich model suggest that higher initial adsorption rate, extent of surface coverage, and activation energy are favored at a lower adsorbent dose. The values of these parameters are reflected in Table 2. The agreement of the results with Elovich model with the observed values is subsequently explained. The adequacy of Elovich model to fit experimental data to heterogeneous catalyst surfaces helps to explain the fit in predicting the adsorption of congo red onto calamansi peels. This form of kinetic law involves a variation of the energetics of chemisorption with the active sites resulting to different activation energies for chemisorption since the peels of calamansi have been found to contain hydroxycinnamic acids and phenolic acids\textsuperscript{33}. Since calamansi and orange belong to the same family, and both peels contain various functional groups; electrostatic attraction, organic properties, and structure of dye molecules can influence the adsorption process. Dried orange peel with pH 4 has higher tendency of electrostatic attraction since congo red has an anionic functional group, a high electrostatic attraction exists between the positively charged surface of the absorbent and the anionic dye\textsuperscript{32}.

The initial parameter estimates for the MacArthur-Wilson model were obtained from the linear plots given in Figure 2(d). The observed and predicted values obtained using the MacArthur-Wilson model are very close to each other as justified by the coefficients of determination which are almost unity as shown in Table 2. This suggests that the adsorption phenomenon can be approximately described using the MacArthur-Wilson model for the different adsorbent doses. However, the rate ($b_1$), at which the uptake approaches its potential maximum is relatively faster at a lower adsorbent dose.

Estimates for the diffusion rate constant and thickness of boundary layer of the intraparticle diffusion model are also reflected in Table 1. The intraparticle diffusion model offers an adequate fit for the experimental data involving higher adsorbent dose. The intraparticle diffusion is noted to be relatively faster at a higher adsorbent dose as a result of the instantaneous utilization of the most readily available adsorbing sites on the adsorbent surface, while the boundary layer effect appeared to be larger at the lower adsorbent dose as described by the linear plots in Figure 2(e).
Elovich model provides the best fit in the uptake of the dye in any adsorbent dose with error values noted to be smaller in the case of lower adsorbent dose as reflected in Table 3. Intraparticle diffusion model offers a better fit involving higher adsorbent dose as justified by small error measures and high coefficients of determination. Identifying the best-fit kinetic model is important in predicting the mechanisms involving chemical reaction or mass transport process that control the rate of the pollutant removal since this information is important in the design of appropriate sorption treatment plants.

Moreover, analysis of the differential forms and the second-order derivatives of the Elovich, MacArthur-Wilson, and intraparticle diffusion models point out that these are negative over the entire range of contact time. These second-order derivatives are presented in Table 4. As such, these models justify the concave downward appearance of the curve when the experimental values on the amount of dye adsorbed from an aqueous solution onto calamansi peels versus contact time are fitted. The graphs of these models are displayed in Figure 3.

CONCLUSION

The removal of congo red reflects a relatively slow initial and final increase rates against contact time. The removal of congo red increases at higher adsorbent dose and longer contact time. The kinetic processes involved behave under a pseudo-second order reaction, based on the assumptions that the rate limiting step, may be chemical adsorption or chemisorption involving valency forces through sharing or exchange of electrons between congo red and calamansi peels. Elovich model suggests that higher initial adsorption rate, extent of surface coverage, and activation energy are favored at a lower adsorbent dose, while the intraparticle diffusion model offers an adequate fit for the experimental data involving higher adsorbent dose. The intraparticle diffusion is noted to be relatively faster at a higher adsorbent dose as a result of the instantaneous utilization of the most readily available adsorbing sites on the adsorbent surface.

Given the results of the study, the removal of congo red from an aqueous solution onto calamansi peels has been found possible. With this information, it is possible to create a design that will optimize a treatment procedure employing calamansi peels as a biosorbent.

REFERENCES


